

Volume--finding missing measurement algebraically

Big Idea: Using the formulas for volume, any one missing measurement can be found algebraically.

*It may be necessary to approximate pi (π) before the end of the problem.

Volume Formulas →

| | | |
|-----------------------------|-----------------------------------|------------------------------------|
| Cylinder $V = \pi r^2 h$ | Cone $V = \frac{\pi r^2 h}{3}$ | Sphere $V = \frac{4\pi r^3}{3}$ |
|-----------------------------|-----------------------------------|------------------------------------|

Examples:

Find the height of a cylinder with a volume of 600m^3 and a radius of 8m.

$$\begin{aligned}
 V &= \pi r^2 h \\
 600 &= \pi 8^2 h \\
 \frac{600}{64} &= \frac{64\pi h}{64} \\
 \frac{9.375}{\pi} &= \frac{\pi h}{\pi} \\
 2.99\text{m} &\approx h
 \end{aligned}$$

Find the radius of a cone with a volume of 300m^3 and a height of 10m.

$$\begin{aligned}
 V &= \frac{\pi r^2 h}{3} & 28.66 \approx r^2 \\
 300 &= \frac{\pi r^2 \cdot 10}{3} & \sqrt{28.66} \approx r \\
 \cdot 3 & & 5.35 \approx r \\
 \frac{900}{10} &= \frac{\pi r^2 \cdot 10}{10} & \text{m} \\
 \frac{90}{\pi} &= \frac{\pi r^2}{\pi}
 \end{aligned}$$

Find the radius of a sphere with a volume of 450cm^3 .

$$\begin{aligned}
 V &= \frac{4\pi r^3}{3} & r^3 \approx 107.48 \\
 450 &= \frac{4\pi r^3}{3} & \sqrt[3]{107.48} \approx r \\
 \cdot 3 & & 4.75 \approx r \\
 \frac{1350}{4} &= \frac{4\pi r^3}{4} & \text{cm} \\
 \frac{337.5}{\pi} &= \frac{\pi r^3}{\pi}
 \end{aligned}$$